Math 17 – Spring 2011 Name:_______________________________
April 6, 2011

Test # 2

Please complete the following problems. Be sure to ask me if you have any questions or anything is unclear. Partial credit will be given, so **please be sure to show all of your work. Please use complete sentences to answer ALL questions.**

The *Z*-Table and *t*-Table are included at the end of the test.

Reliability of Spot Test Kits for Detecting Lead[1]

There has been a long-standing need for a technique that can provide fast, accurate and precise results regarding the presence of hazardous levels of lead in settled house dust. Several home testing kits are now available. One kit manufactured by Hybrivet (LeadCheck Swabs) is advertised as able to detect lead dust levels that exceed the U.S. Environmental Protection Agency's dust lead standard for floors (40 $\mu g/ft^2$).

You would like investigate Hybrivet's claims. You are interested in the proportion of test swabs that correctly detect high lead dust levels.

1. You'd like to find a 95% confidence interval for the proportion of swabs that correctly detect high lead dust levels to within 5 percentage points. Your budget is $600. If it costs $3 per test strip to do the test, will you be able to take the needed sample?

2. If you were to estimate the confidence interval to within 5 percentage points using a sample of 200 swabs, what would be the confidence level of that interval?

3. Due to the budgetary constraints given above, you take a random sample of 200 test swabs. It is reasonable here to assume the different swabs are independent. You find that 46 of the swabs test positive for high lead. Estimate and interpret a 95% confidence interval for the true proportion of positive test results.

[1] Korfmacher, K.S. and Dixon, S., "Reliability of Spot Test Kits for Detecting Lead in Household Dust," Environmental Research, 2007 June, 104 (2): 241-249.

Reliability of Spot Test Kits for Detecting Lead (continued)

4. We'll test the following hypotheses for a single test strip.

$$H_0\text{: Lead is absent}$$
$$H_A\text{: Lead is present}$$

   From the perspective of this test, describe the errors that could occur and describe which one is more important to minimize.

5. True/False. If you consider a ***specific*** 95% confidence interval for a population proportion, then there is a 95% chance that the population proportion lies within that interval.

   True ***False***

6. True/False. The probability the 95% CI computed above contains the sample proportion of correct test swabs is 0.95.

   True ***False***

7. Suppose we are doing a one-proportion *Z*-test to test if a majority of people in Massachusetts were born here. We sample 50 people and use an α = 0.10 cutoff to test

$$H_0: p = 0.65$$
$$H_A: p < 0.65.$$

   What is the power of this test if the true underlying proportion is actually 0.40?

Name that Scenario – For each scenario, determine and define the parameter of interest and state which procedure is most appropriate. If you choose hypothesis test, provide the null and alternative hypothesis. All questions relate to a data set collected on bulls sold at auction. Variables include: breed (Angus, Hereford, Simental), yearling height at shoulder, percent fat-free body weight, sale height at shoulder and sale weight.

8. Research question: Is there a difference in average sale weight for Angus versus Simental bulls?

9. Research question: Estimate the fraction of Hereford bulls sold at auction with an interval.

10. Research question: Test if the percent of fat free body weight for bulls sold at auction is greater than 70 percent.

11. Research question: Estimate the average sale weight for bulls sold at auction with an interval.

12. Research question: Test whether there a height increase bulls when comparing their sale height to yearling height?

13. Research question: Test whether a higher percentage of Angus bulls have at least 68 percent fat free body weight compared to Hereford bulls?

Cholesterol in Urban and Rural Guatemalans[2]

In 1964 there was a study that contrasted cholesterol levels between urban and rural Guatemalans. The data along with some summary statistics and graphs of the data are shown below. We can assume that these are both random samples, and that the subjects are independent between and within groups.

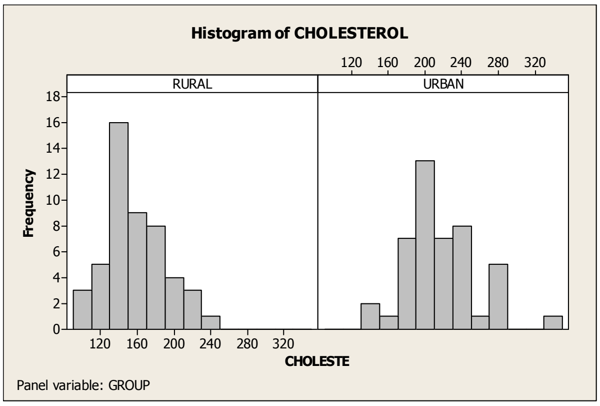
Cholesterol levels in urban and rural guatemalans

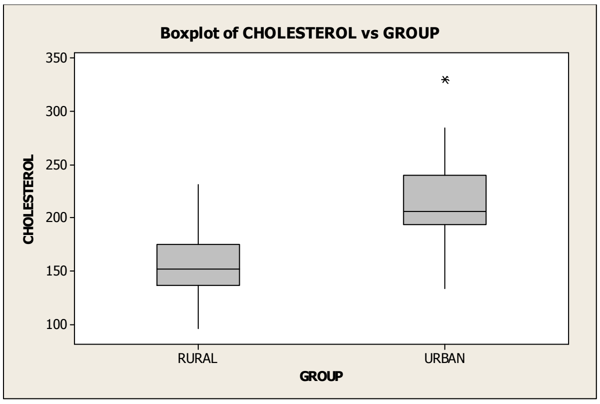
Serum total cholesterol (mg/l) levels among *urban* residents (n=45)
133 134 155 170 175 179 181 184 188 189 190 196 197 199 200 200 201 201 204 205
205 205 206 214 217 222 222 227 227 228 234 234 236 239 241 242 244 249 252 273
279 284 284 284 330

Serum total cholesterol (mg/l) levels among *rural* residents (n—49)
95 108 108 114 115 124 129 129 131 131 135 136 136 139 140 142 142 143 143 144
144 145 145 148 152 152 155 157 158 158 162 165 166 171 172 173 174 175 180 181
189 192 194 197 204 220 223 226 231

Descriptive Statistics: CHOLESTEROL

Variable	GROUP	n	Mean	StDev
CHOLESTEROL	RURAL	49	157.00	31.76
	URBAN	45	216.87	39.92





14. State the hypotheses to test whether the mean cholesterol level of the urban group is greater than that of the rural group.

15. Conduct the test, if appropriate, and state your conclusion. You may assume that the degrees of freedom are $df = \frac{\left(\frac{s_1^2}{n_1}+\frac{s_2^2}{n_2}\right)^2}{\frac{1}{n_1-1}\left(\frac{s_1^2}{n_1}\right)^2+\frac{1}{n_2-1}\left(\frac{s_2^2}{n_2}\right)^2} = 84.002$

[2] Example taken from F. L. Ramsey and D. W. Schafer, The Statistics Sleuth, A Course in Methods of Data Analysis, 2nd edition, Duxbury Press 2002.

Schizophrenia[3]

A study of schizophrenia was interested in whether there are any physiological factors associated with schizophrenia. In particular, are there size differences in certain areas of the brain? A twin study measured the left hippocampus volume of 15 pairs of twins where one of them was schizophrenic and the other wasn't. The measurements were made using MRI.

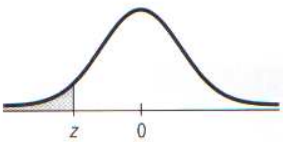
We wish to test whether there is a difference in left hippocampus volume between the two groups of measurements. Using a "shotgun" approach, the output from several Rcmdr procedures is given below. You may assume that all necessary conditions are satisfied.

16. Give the appropriate *p*-value for this test and make a conclusion.

Welch Two Sample t-test data: Volume by Condition t = -1.9898, df = 26.775, p-value = 0.05691 alternative hypothesis: true difference in means is not equal to 0 95 percent confidence interval: -0.403606427 0.006273094 sample estimates: mean in Affected mean in Unaffected 1.56000 1.758667	One Sample t-test data: schizophrenia$Volume t = 31.6629, df = 29, p-value < 2.2e-16 alternative hypothesis: true mean is not equal to 0 95 percent confidence interval: 1.552150 1.766516 sample estimates: mean of x 1.659333
Paired t-test data: matchit$Affected and matchit$Unaffected t = 3.2289, df = 14, p-value = 0.006062 alternative hypothesis: true difference in means is not equal to 0 95 percent confidence interval: 0.0667041 0.3306292 sample estimates: mean of the differences 0.1986667	1-sample proportions test data: rbind(.Table), null probability 0.5 X-squared = 0, df = 1, p-value = 1 alternative hypothesis: true p is not equal to 0.5 95 percent confidence interval: 0.3315413 0.6684587 sample estimates: p 0.5

[3] Example taken from F. L. Ramsey and D. W. Schafer, The Statistics Sleuth, A Course in Methods of Data Analysis, 2nd edition, Duxbury Press 2002.

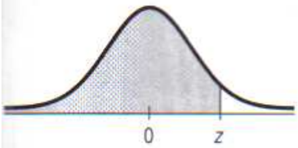
Table Z
Areas under the standard Normal curve



Second decimal place in z										
0.09	*0.08*	*0.07*	*0.06*	*0.05*	*0.04*	*0.03*	*0.02*	*0.01*	*0.00*	*z*
									0.0000†	−3.9
0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	−3.8
0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	−3.7
0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0002	0.0002	−3.6
0.0002	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002	−3.5
0.0002	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	−3.4
0.0003	0.0004	0.0004	0.0004	0.0004	0.0004	0.0004	0.0005	0.0005	0.0005	−3.3
0.0005	0.0005	0.0005	0.0006	0.0006	0.0006	0.0006	0.0006	0.0007	0.0007	−3.2
0.0007	0.0007	0.0008	0.0008	0.0008	0.0008	0.0009	0.0009	0.0009	0.0010	−3.1
0.0010	0.0010	0.0011	0.0011	0.0011	0.0012	0.0012	0.0013	0.0013	0.0013	−3.0
0.0014	0.0014	0.0015	0.0015	0.0016	0.0016	0.0017	0.0018	0.0018	0.0019	−2.9
0.0019	0.0020	0.0021	0.0021	0.0022	0.0023	0.0023	0.0024	0.0025	0.0026	−2.8
0.0026	0.0027	0.0028	0.0029	0.0030	0.0031	0.0032	0.0033	0.0034	0.0035	−2.7
0.0036	0.0037	0.0038	0.0039	0.0040	0.0041	0.0043	0.0044	0.0045	0.0047	−2.6
0.0048	0.0049	0.0051	0.0052	0.0054	0.0055	0.0057	0.0059	0.0060	0.0062	−2.5
0.0064	0.0066	0.0068	0.0069	0.0071	0.0073	0.0075	0.0078	0.0080	0.0082	−2.4
0.0084	0.0087	0.0089	0.0091	0.0094	0.0096	0.0099	0.0102	0.0104	0.0107	−2.3
0.0110	0.0113	0.0116	0.0119	0.0122	0.0125	0.0129	0.0132	0.0136	0.0139	−2.2
0.0143	0.0146	0.0150	0.0154	0.0158	0.0162	0.0166	0.0170	0.0174	0.0179	−2.1
0.0183	0.0188	0.0192	0.0197	0.0202	0.0207	0.0212	0.0217	0.0222	0.0228	−2.0
0.0233	0.0239	0.0244	0.0250	0.0256	0.0262	0.0268	0.0274	0.0281	0.0287	−1.9
0.0294	0.0301	0.0307	0.0314	0.0322	0.0329	0.0336	0.0344	0.0351	0.0359	−1.8
0.0367	0.0375	0.0384	0.0392	0.0401	0.0409	0.0418	0.0427	0.0436	0.0446	−1.7
0.0455	0.0465	0.0475	0.0485	0.0495	0.0505	0.0516	0.0526	0.0537	0.0548	−1.6
0.0559	0.0571	0.0582	0.0594	0.0606	0.0618	0.0630	0.0643	0.0655	0.0668	−1.5
0.0681	0.0694	0.0708	0.0721	0.0735	0.0749	0.0764	0.0778	0.0793	0.0808	−1.4
0.0823	0.0838	0.0853	0.0869	0.0885	0.0901	0.0918	0.0934	0.0951	0.0968	−1.3
0.0985	0.1003	0.1020	0.1038	0.1056	0.1075	0.1093	0.1112	0.1131	0.1151	−1.2
0.1170	0.1190	0.1210	0.1230	0.1251	0.1271	0.1292	0.1314	0.1335	0.1357	−1.1
0.1379	0.1401	0.1423	0.1446	0.1469	0.1492	0.1515	0.1539	0.1562	0.1587	−1.0
0.1611	0.1635	0.1660	0.1685	0.1711	0.1736	0.1762	0.1788	0.1814	0.1841	−0.9
0.1867	0.1894	0.1922	0.1949	0.1977	0.2005	0.2033	0.2061	0.2090	0.2119	−0.8
0.2148	0.2177	0.2206	0.2236	0.2266	0.2296	0.2327	0.2358	0.2389	0.2420	−0.7
0.2451	0.2483	0.2514	0.2546	0.2578	0.2611	0.2643	0.2676	0.2709	0.2743	−0.6
0.2776	0.2810	0.2843	0.2877	0.2912	0.2946	0.2981	0.3015	0.3050	0.3085	−0.5
0.3121	0.3156	0.3192	0.3228	0.3264	0.3300	0.3336	0.3372	0.3409	0.3446	−0.4
0.3483	0.3520	0.3557	0.3594	0.3632	0.3669	0.3707	0.3745	0.3783	0.3821	−0.3
0.3859	0.3897	0.3936	0.3974	0.4013	0.4052	0.4090	0.4129	0.4168	0.4207	−0.2
0.4247	0.4286	0.4325	0.4364	0.4404	0.4443	0.4483	0.4522	0.4562	0.4602	−0.1
0.4641	0.4681	0.4721	0.4761	0.4801	0.4840	0.4880	0.4920	0.4960	0.5000	−0.0

†For $z \leq -3.90$, the areas are 0.0000 to four decimal places.

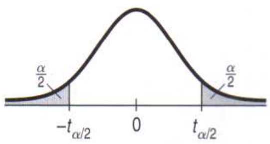
Table Z (cont.)
Areas under the standard Normal curve



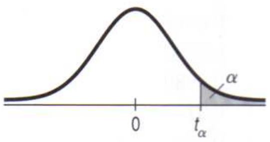
	Second decimal place in z									
z	*0.00*	*0.01*	*0.02*	*0.03*	*0.04*	*0.05*	*0.06*	*0.07*	*0.08*	*0.09*
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990
3.1	0.9990	0.9991	0.9991	0.9991	0.9992	0.9992	0.9992	0.9992	0.9993	0.9993
3.2	0.9993	0.9993	0.9994	0.9994	0.9994	0.9994	0.9994	0.9995	0.9995	0.9995
3.3	0.9995	0.9995	0.9995	0.9996	0.9996	0.9996	0.9996	0.9996	0.9996	0.9997
3.4	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9998
3.5	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998
3.6	0.9998	0.9998	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999
3.7	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999
3.8	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999
3.9	1.0000†									

†For $z \geq 3.90$, the areas are 1.0000 to four decimal places.

Table T
Values of t_α



Two tails



One tail

Two-tail probability	0.20	0.10	0.05	0.02	0.01	
One-tail probability	0.10	0.05	0.025	0.01	0.005	
df						df
1	3.078	6.314	12.706	31.821	63.657	1
2	1.886	2.920	4.303	6.965	9.925	2
3	1.638	2.353	3.182	4.541	5.841	3
4	1.533	2.132	2.776	3.747	4.604	4
5	1.476	2.015	2.571	3.365	4.032	5
6	1.440	1.943	2.447	3.143	3.707	6
7	1.415	1.895	2.365	2.998	3.499	7
8	1.397	1.860	2.306	2.896	3.355	8
9	1.383	1.833	2.262	2.821	3.250	9
10	1.372	1.812	2.228	2.764	3.169	10
11	1.363	1.796	2.201	2.718	3.106	11
12	1.356	1.782	2.179	2.681	3.055	12
13	1.350	1.771	2.160	2.650	3.012	13
14	1.345	1.761	2.145	2.624	2.977	14
15	1.341	1.753	2.131	2.602	2.947	15
16	1.337	1.746	2.120	2.583	2.921	16
17	1.333	1.740	2.110	2.567	2.898	17
18	1.330	1.734	2.101	2.552	2.878	18
19	1.328	1.729	2.093	2.539	2.861	19
20	1.325	1.725	2.086	2.528	2.845	20
21	1.323	1.721	2.080	2.518	2.831	21
22	1.321	1.717	2.074	2.508	2.819	22
23	1.319	1.714	2.069	2.500	2.807	23
24	1.318	1.711	2.064	2.492	2.797	24
25	1.316	1.708	2.060	2.485	2.787	25
26	1.315	1.706	2.056	2.479	2.779	26
27	1.314	1.703	2.052	2.473	2.771	27
28	1.313	1.701	2.048	2.467	2.763	28
29	1.311	1.699	2.045	2.462	2.756	29
30	1.310	1.697	2.042	2.457	2.750	30
32	1.309	1.694	2.037	2.449	2.738	32
35	1.306	1.690	2.030	2.438	2.725	35
40	1.303	1.684	2.021	2.423	2.704	40
45	1.301	1.679	2.014	2.412	2.690	45
50	1.299	1.676	2.009	2.403	2.678	50
60	1.296	1.671	2.000	2.390	2.660	60
75	1.293	1.665	1.992	2.377	2.643	75
100	1.290	1.660	1.984	2.364	2.626	100
120	1.289	1.658	1.980	2.358	2.617	120
140	1.288	1.656	1.977	2.353	2.611	140
180	1.286	1.653	1.973	2.347	2.603	180
250	1.285	1.651	1.969	2.341	2.596	250
400	1.284	1.649	1.966	2.336	2.588	400
1000	1.282	1.646	1.962	2.330	2.581	1000
∞	1.282	1.645	1.960	2.326	2.576	∞
Confidence levels	80%	90%	95%	98%	99%	